



Bayesian Calibration

George Hripcsak, David Madigan,
Jami Jackson Mulgrave



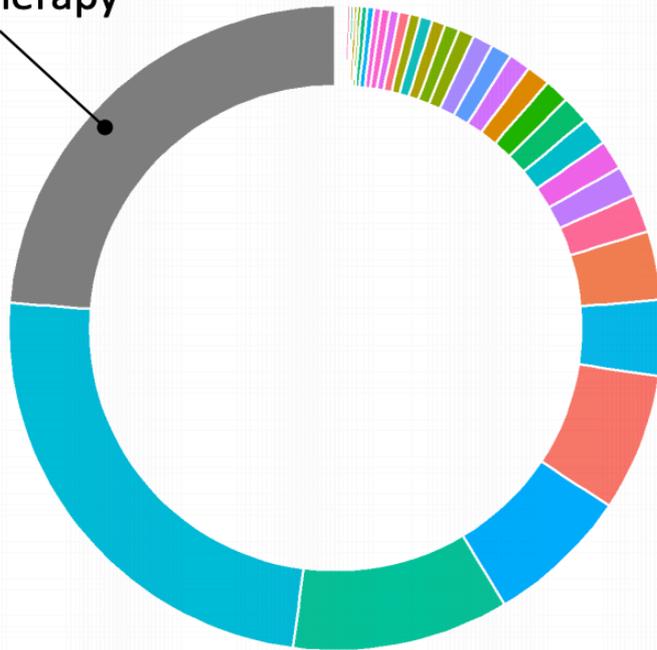
LEGEND

- Reproducible, systematized, open source approach at scale
- Negative controls
 - Drugs and outcomes “known” to have no causal association
 - Literature, product labels, spontaneous reports
 - Empirical p-values
- Positive Controls
 - Inject signals onto negative controls with known effect size
 - Calibrated confidence intervals



Hypertension mono-therapy

Duo-therapy



- | | |
|---------------------|-----------------|
| Amlodipine | Labetalol |
| Atenolol | Lisinopril |
| Azilsartan | Losartan |
| Benazepril | Methyldopa |
| Bisoprolol | Metoprolol |
| Candesartan | Nadolol |
| Captopril | Nebivolol |
| Carvedilol | Nicardipine |
| Chlorthalidone | Nifedipine |
| Clonidine | Olmesartan |
| Diltiazem | Propranolol |
| Doxazosin | Quinapril |
| Enalapril | Ramipril |
| Felodipine | Spiroinolactone |
| Fosinopril | Telmisartan |
| Furosemide | Terazosin |
| Hydralazine | Torsemide |
| Hydrochlorothiazide | Valsartan |
| Indapamide | Verapamil |
| irbesartan | |

Truven Health MarketScan CCAE. Therapies > 2 ingredients not shown



58 outcomes of interest

Abdominal pain	Dementia	Ischemic stroke
Abnormal weight gain	Depression	Kidney disease
Abnormal weight loss	Diarrhea	Malignant neoplasm
Acute myocardial infarction	Edema	Measured renal dysfunction
Acute pancreatitis	End stage renal disease	Nausea
Acute renal failure	Fall	Neutropenia or agranulocytosis
All-cause mortality	Gastrointestinal bleeding	Rash
Anaphylactoid reaction	Gout	Rhabdomyolysis
Anemia	Headache	Stroke
Angioedema	Heart failure	Sudden cardiac death
Anxiety	Hemorrhagic stroke	Syncope
Bradycardia	Hepatic failure	Thrombocytopenia
Cardiac arrhythmia	Hospitalization with heart failure	Transient ischemic attack
Cardiovascular disease	Hospitalization with preinfarction syndrome	Type 2 diabetes mellitus
Cardiovascular-related mortality	Hyperkalemia	Vasculitis
Chest pain or angina	Hypokalemia	Venous thromboembolic events
Chronic kidney disease	Hypomagnesemia	Vertigo
Coronary heart disease	Hyponatremia	Vomiting
Cough	Hypotension	
Decreased libido	Impotence	



76 negative controls

Abnormal cervical smear	Disproportion of reconstructed breast	Nicotine dependence
Abnormal pupil	Effects of hunger	Noise effects on inner ear
Abrasion and/or friction burn of trunk without infection	Endometriosis	Nonspecific tuberculin test reaction
Absence of breast	Epidermoid cyst	Non-toxic multinodular goiter
Absent kidney	Feces contents abnormal	Onychomycosis due to dermatophyte
Acid reflux	Foreign body in orifice	Opioid abuse
Acquired hallux valgus	Ganglion cyst	Passing flatus
Acquired keratoderma	Genetic predisposition	Postviral fatigue syndrome
Acquired trigger finger	Hammer toe	Presbyopia
Acute conjunctivitis	Hereditary thrombophilia	Problem related to lifestyle
Amputated foot	Herpes zoster without complication	Psychalgia
Anal and rectal polyp	High risk sexual behavior	Ptotic breast
Burn of forearm	Homocystinuria	Regular astigmatism
Calcaneal spur	Human papilloma virus infection	Senile hyperkeratosis
Cannabis abuse	Ileostomy present	Somatic dysfunction of lumbar region
Cervical somatic dysfunction	Impacted cerumen	Splinter of face, without major open wound
Changes in skin texture	Impingement syndrome of shoulder region	Sprain of ankle
Chondromalacia of patella	Ingrowing nail	Strain of rotator cuff capsule
Cocaine abuse	Injury of knee	Tear film insufficiency
Colostomy present	Irregular periods	Tobacco dependence syndrome
Complication due to Crohn's disease	Kwashiorkor	Vaginitis and vulvovaginitis
Contact dermatitis	Late effect of contusion	Verruca vulgaris
Contusion of knee	Late effect of motor vehicle accident	Wrist joint pain
Crohn's disease	Leukorrhea	Wristdrop
Derangement of knee	Macular drusen	
Difficulty sleeping	Melena	



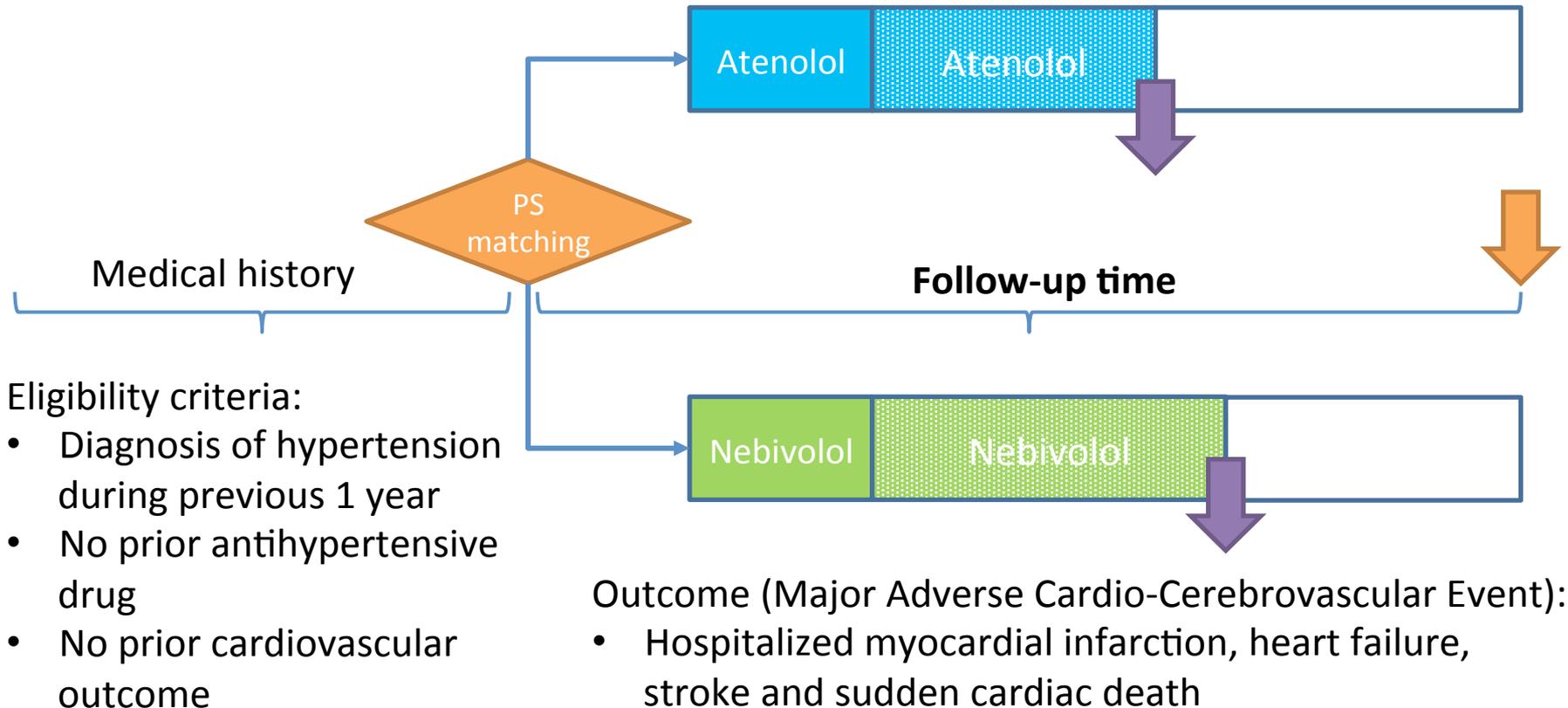
Method: Study design (LEGEND)

Treatment strategies:

- **Atenolol**
- **Nebivolol**

Causal contrasts of interest:

- On-treatment effect
- Intent-to-treat effect



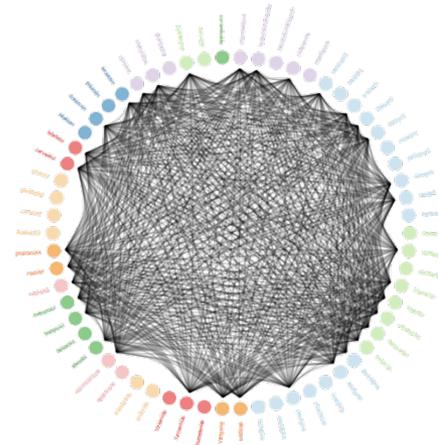
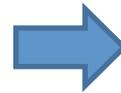
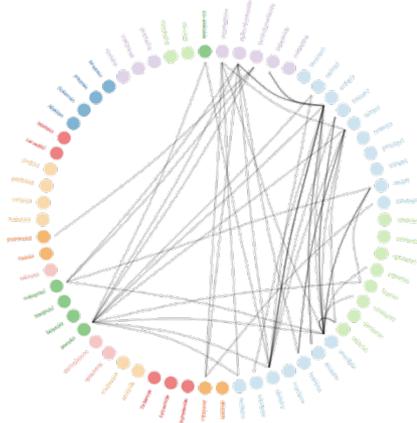


Method: **LEGEND** (Large-scale Evidence Generation and Evaluation in a Network of Databases)

All randomized trials

LEGEND

40 trials



10,278 comparisons

US Insurance databases

IBM® MarketScan® CCAE (Commercial Claims and Encounters)

IBM® MarketScan® MDCD (Multi-state Medicaid)

IBM® MarketScan® MDCR (Medicare Supplemental Beneficiaries)

Optum® Clinformatics®

Japanese insurance database

Japan Medical Data Center (JMDC)

Korean National insurance database

NHIS-national sample cohort (NHIS-NSC) DB

US EHR databases

Columbia University medical Center

Optum® PANTHER®

German EHR database

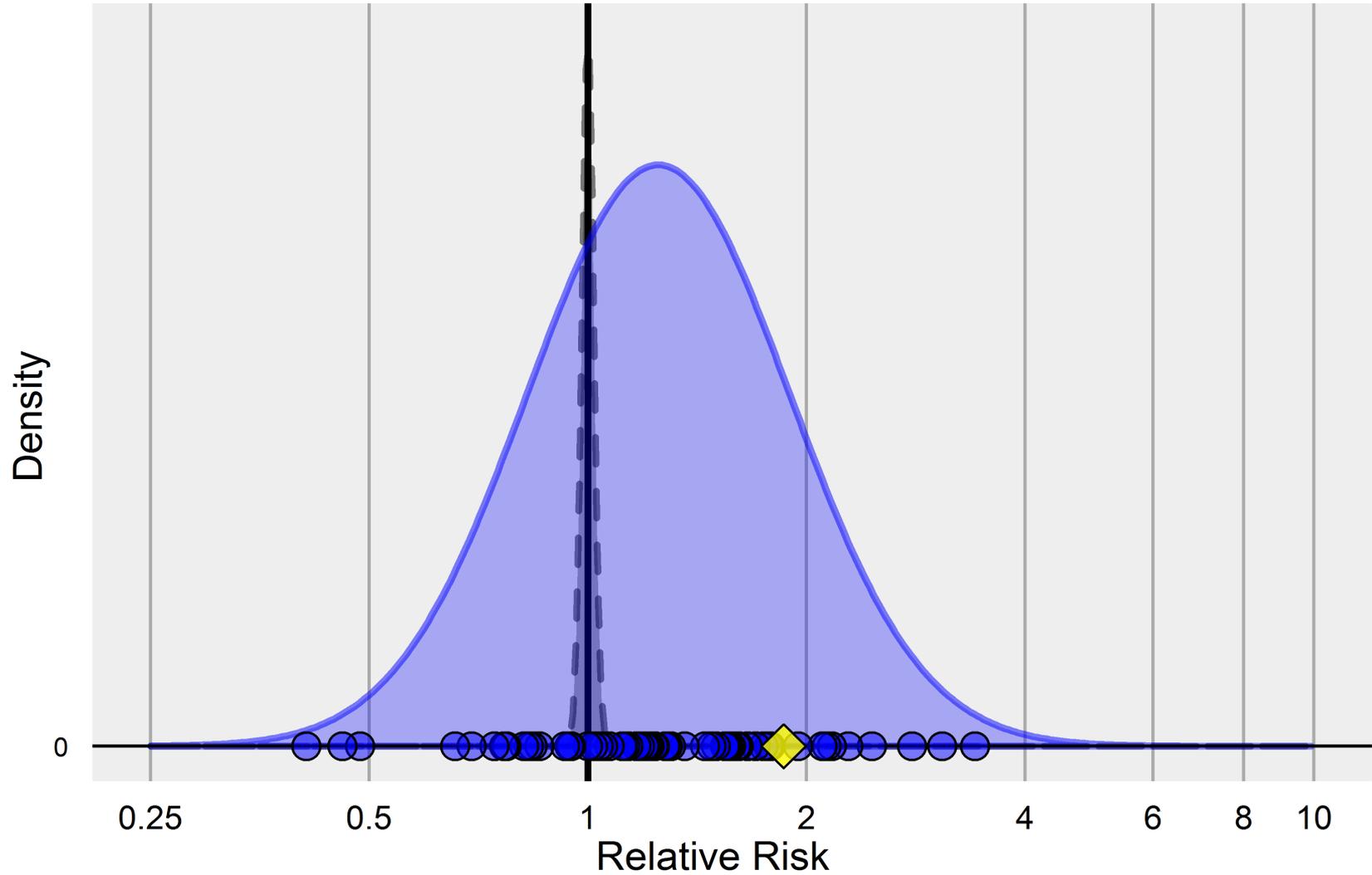
QuintilesIMS Disease Analyzer (DA) Germany

<https://github.com/OHDSI/LEGEND>



Negative controls & the null distribution

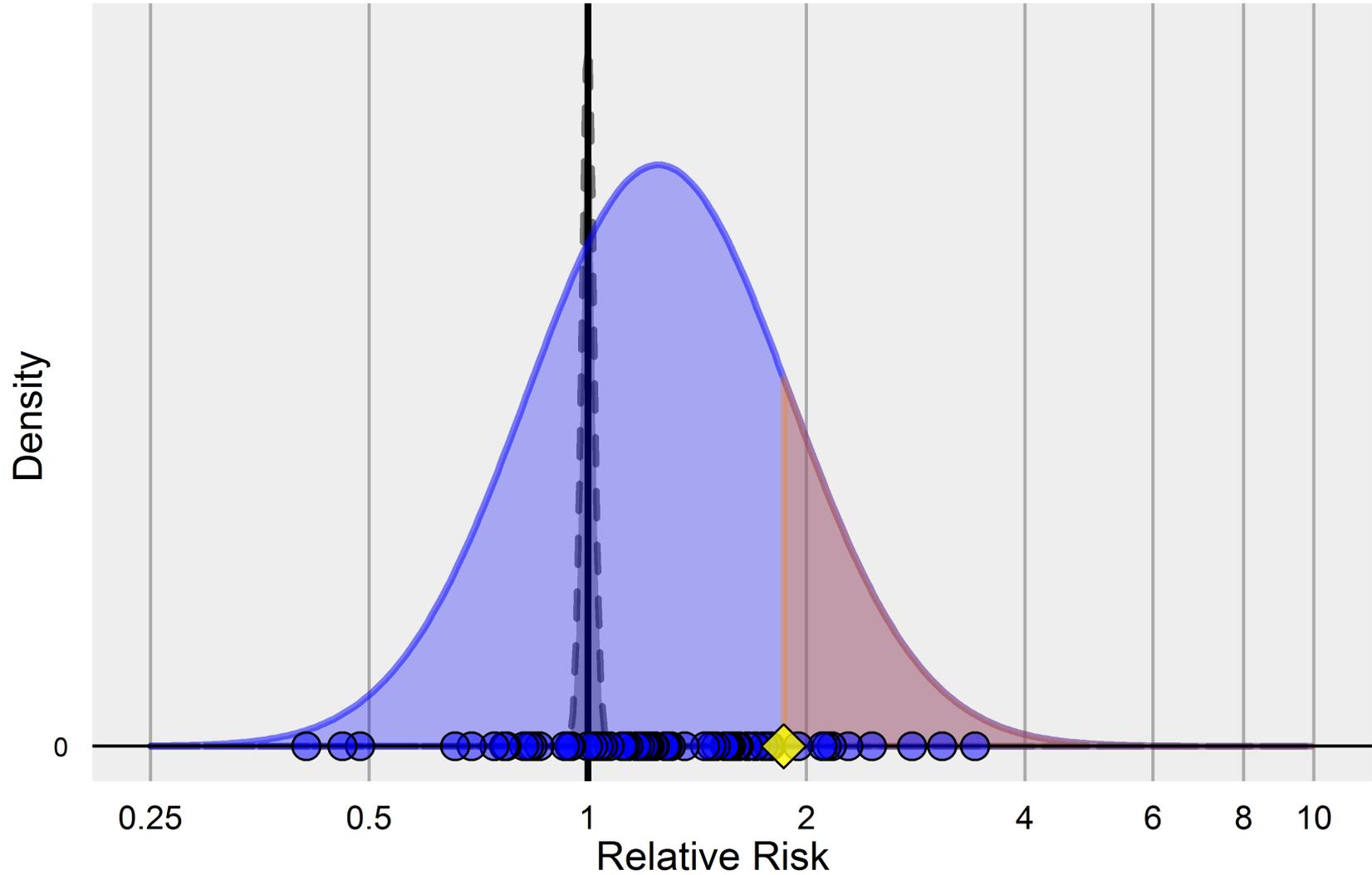
CC: 2000314, CCAE, GI Bleed





Negative controls & the null distribution

CC: 2000314, CCAE, GI Bleed





Bayesian Approach

- Compute the posterior distribution of the TCO effect of interest, conditional on:
 - Directly estimated effect for the TCO
 - Estimated effects on all negative and positive controls
 - Across all databases
 - Across all “methods” (e.g. matching versus stratification)
 - MCMC
-



One model, one database (V1)

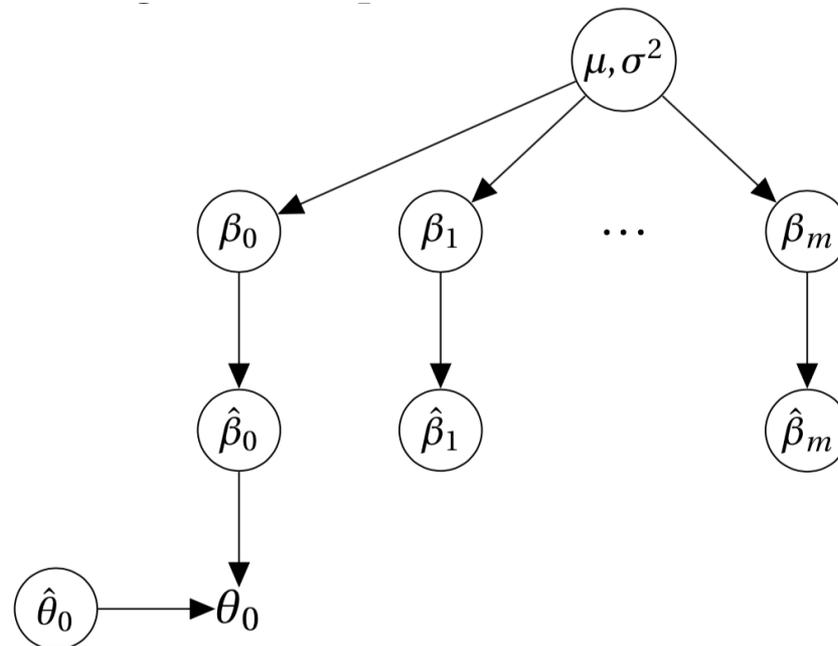
θ_0 true effect size of interest

θ_i true effect size for the controls, $i = 1, \dots, m$

$\hat{\theta}_i$ estimated effect sizes, $i = 0, \dots, m$

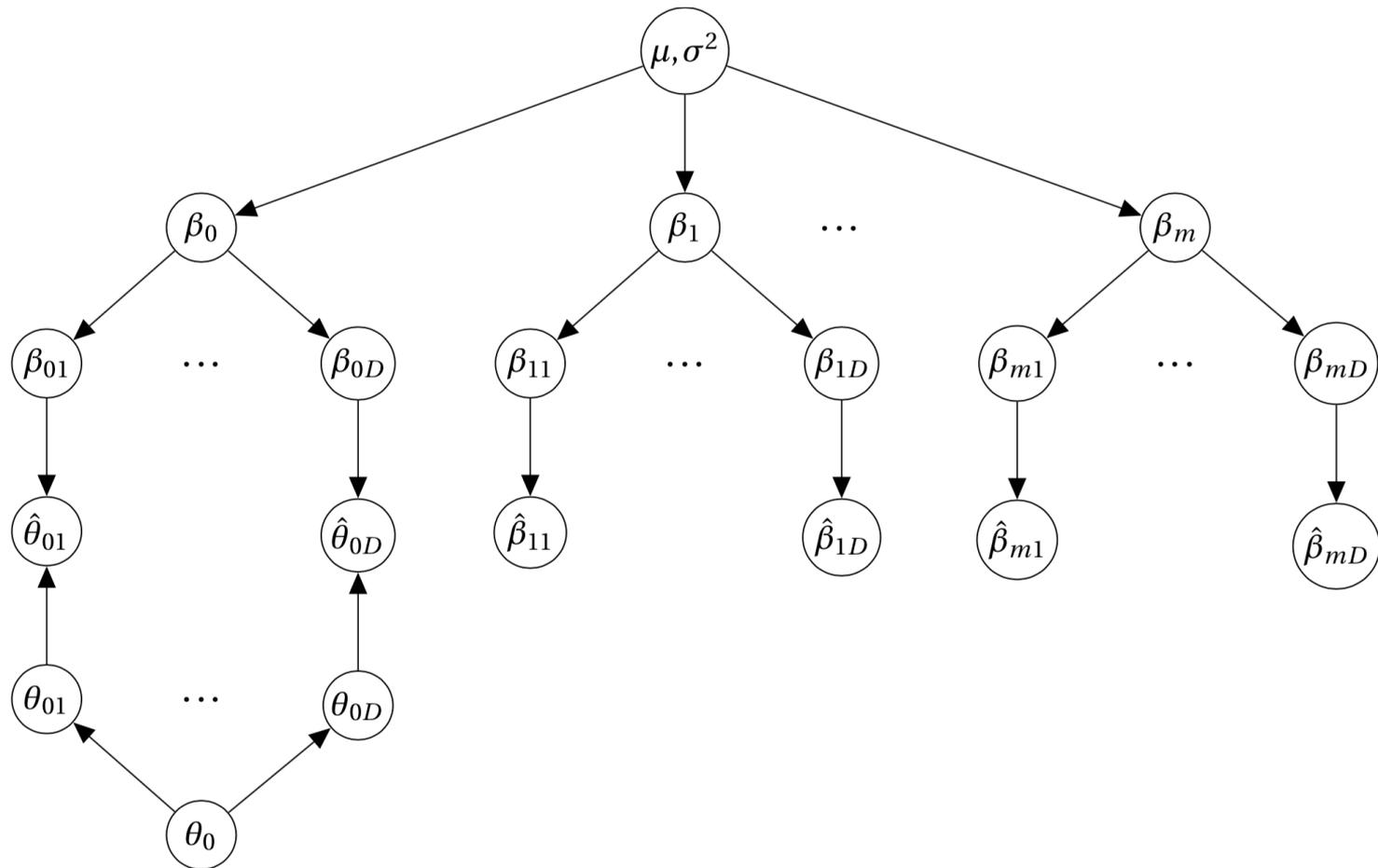
$\hat{\beta}_i = \hat{\theta}_i - \theta_i$ "estimated bias," $i = 0, \dots, m$

$E[\hat{\beta}_i] = \beta_i$ $i = 0, \dots, m$





One model, many databases (V2)



Combining calibration with random effects meta-analysis



Many models, many databases (V4, BMA)

$$p(\theta_0|\mathcal{D}) = \sum_k p(\theta_0|M_k, \mathcal{D}) p(M_k|\mathcal{D})$$

where the data, \mathcal{D} , comprise:

$$\hat{\theta}_{0j}^k, k = 1, \dots, M, j = 1, \dots, D$$

$$\hat{\theta}_{ij}^k, k = 1, \dots, M, j = 1, \dots, D, i = 1, \dots, Q$$

$$\theta_i, i = 1, \dots, Q$$

can show that: $p(M_k|\mathcal{D}) \propto \prod_{i=1}^Q \prod_{j=1}^D p(\hat{\theta}_{ij}^k|\theta_i, M_k)$

Combining calibration with random effects meta-analysis and BMA



Initial results (V1)

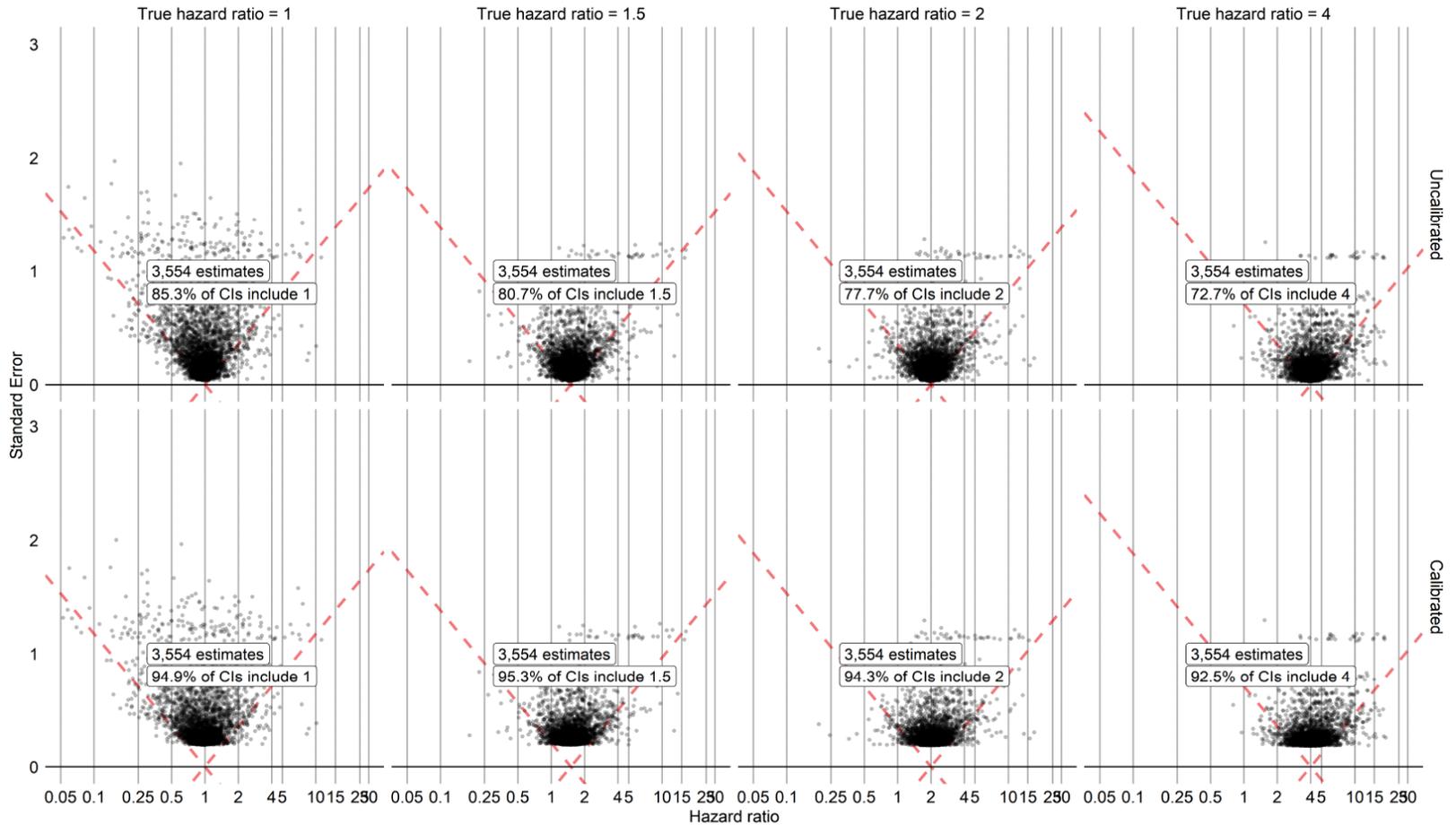


Figure: Optum Database Results



Root Mean Squared Error Using 95%

